

# Formal Verification of Probabilistic Systems

## ERRATA

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## Abbreviations

**lft:** Lines from top (equations, section titles, etc included, page headers not included).

**lfb:** Lines from bottom (equations, section titles, etc included).

**eq:** Numbered equation

## Errata

p. vi, lft 7

**Error:** readings and orals committee

**Correction:** reading and orals committees

p. 45, lft 14

**Error:**  $sa(C, D) \subset sa(C'', D'') \subseteq (C, D)$

**Correction:**  $sa(C, D) \subset sa(C'', D'') \subseteq sa(C', D')$

p. 52, lft 4

**Error:**  $s \in S - U$

**Correction:**  $s \in S - U, a \in A(s)$

p. 52, lft 8

**Error:** *iff*

**Correction:** *if*

p. 56, lfb 9

**Error:** Let  $B'$  be the set of states that cannot reach  $S_\phi$  in the graph  $(S', \rho_{(S', A')})$ .

**Correction:** Let  $B'$  be the subset of states of  $S'$  that cannot reach  $U$  in the graph  $(S', \rho_{(S', A')})$ .

p. 56, lfb 5

**Error:**  $s \notin S_\phi$

**Correction:**  $s \notin U$

p. 64, lfb 2

**Error:** If  $a \in A(s)$

**Correction:** If  $a \in A(s) - D_i(s)$

p. 64, lfb 7

**Error:** *Fact 1. If  $\mathbf{v}^\bullet = \tilde{L}\mathbf{v}^\bullet$  is a fixpoint of  $\tilde{L}$ , and  $s, t \in B_i$ , for  $1 \leq i \leq n$ , then  $v_s^\bullet = v_t^\bullet$ .*

**Correction:** *Fact 1. If  $\mathbf{v} = \tilde{L}\mathbf{v}$  is a fixpoint of  $\tilde{L}$ , and  $s, t \in B_i$ , for  $1 \leq i \leq n$ , then  $v_s = v_t$ .*

- p. 65, eq (3.21)  
**Error:**  $\arg \max_{a \in \tilde{A}}$   
**Correction:**  $\arg \max_{a \in \tilde{A}(s)}$
- p. 66, lft 1  
**Error:**  $s \neq t_i$  (where  $\langle t_i, a_i \rangle$ )  
**Correction:**  $s \neq u_i$  (where  $\langle u_i, a_i \rangle$ )
- p. 66, lft 4  
**Error:**  $s = t_i$   
**Correction:**  $s = u_i$
- p. 93, lft 5  
**Error:** distinguished initial state  
**Correction:** distinguished set of initial states
- p. 93, lfb 8  
**Error:** for all  $u, v_1, v_2 \in V$   
**Correction:** for all  $u, v_1, v_2 \in V$  with  $v_1 \neq v_2$
- p. 93, lfb 5  
**Error:** for every  $v \in V$   
**Correction:** for every  $u \in V$
- p. 95, lft 9  
**Error:**  $\langle s, u \rangle$   
**Correction:**  $\langle s, u \rangle \in S \times V$
- p. 106, lft 12–13  
**Error:** The transformation does not change the state space of  $\Pi_i$ , and it does not affect the long-run average outcome of experiments.  
**Correction:** The transformation does not affect the long-run average outcome of experiments.
- p. 106, lft 15  
**Error:** do not diverge to  $-\infty$  or  $+\infty$   
**Correction:** do not diverge to  $+\infty$
- p. 106, lfb 8  
**Error:**  $(M_s \subseteq \mathcal{L})$   
**Correction:**  $(M_s \subseteq K^+)$
- p. 108, lft 8  
**Error:** (computation of  $\lambda^-$ )  
**Correction:** (computation of  $\lambda^+$ )
- p. 111, lft 4  
**Error:**  $t \in \bigcup_{a \in A(s)} \text{Succ}(s, a)$   
**Correction:**  $t \in \bigcup_{a \in C(s)} \text{Succ}(s, a)$
- p. 111, lft 7  
**Error:**  $\bigcup_{a \in A(s)}$   
**Correction:**  $\bigcup_{a \in C(s)}$
- p. 111, lft 11  
**Error:**  $\Pr_{\langle s, v \rangle}^\eta$   
**Correction:**  $\Pr_s^\eta$

p. 128, lft 5

**Error:** From the sequence  $\{n_k\}_{k \geq 0}$  we can extract a subsequence  $\{n_l\}_{l \geq 0}$  such that  $\lim_{l \rightarrow \infty} \mathbf{u}_{s, n_l}^\eta = \mathbf{u}$ , for some  $\mathbf{u} \in \bar{U}$ .

**Correction:** From the sequence  $\{n_k\}_{k \geq 0}$  we can extract a subsequence  $\{n_l\}_{l \geq 0}$  such that  $\lim_{l \rightarrow \infty} \mathbf{u}_{s, n_l}^\eta = \mathbf{u}$ . By [Der70, Chapter 7, Theorem 2], it is  $\mathbf{u} \in \bar{U}$ .

p. 150, lft 15

**Error:**  $[v_{s_1} \ v_{s_2} \ v_{s_3} \ v_{s_4}]^t$

**Correction:**  $[v_{s_1} \ v_{s_2} \ v_{s_3}]^t$

p. 150, lft 16

**Error:**  $[3 \ 2 \ 2 \ 1]^t - x[1 \ 1 \ 1 \ 0]^t$

**Correction:**  $\mathbf{v}(x) = [3 \ 2 \ 2]^t - x[1 \ 1 \ 1]^t$

p. 155, lft 8

**Error:**  $\sum_{t \in S-U} p_{st}(a) v_t$

**Correction:**  $\sum_{t \in S-U} p_{st}(a) v_t^\bullet$

p. 156, lft 1

**Error:** Let  $\tilde{L}$  be the operator defined for  $\tilde{\Pi}$  in the same way as  $L$  for  $\Pi$ , and let  $\mathbf{v}^\bullet = \tilde{L}\mathbf{v}^\bullet$  be a fixpoint of  $\tilde{L}$ .

**Correction:** Let  $\tilde{L}$  be the operator defined for  $\tilde{\Pi}$  in the same way as  $L$  for  $\Pi$ .

p. 156, lft 12

**Error:** *Fact 1. If  $\mathbf{v}^\bullet = \tilde{L}\mathbf{v}^\bullet$  is a fixpoint of  $\tilde{L}$ , and  $s, t \in B_i$ , for  $1 \leq i \leq n$ , then  $v_s^\bullet = v_t^\bullet$ .*

**Correction:** *Fact 1. If  $\mathbf{v} = \tilde{L}\mathbf{v}$  is a fixpoint of  $\tilde{L}$ , and  $s, t \in B_i$ , for  $1 \leq i \leq n$ , then  $v_s = v_t$ .*

p. 157, lft 5

**Error:**  $\sum_{t \in S-U} \tilde{p}_{st}(\eta(s)) v_t + \sum_{t \in U} \tilde{p}_{st}(\eta(s)) g(t)$

**Correction:**  $\sum_{t \in S-U} p_{st}(\eta(s)) v_t + \sum_{t \in U} p_{st}(\eta(s)) g(t)$

p. 157, lft 8

**Error:**  $s \neq t_i$  (where  $\langle t_i, a_i \rangle$ )

**Correction:**  $s \neq u_i$  (where  $\langle u_i, a_i \rangle$ )

p. 157, lft 12

**Error:**  $s = t_i$

**Correction:**  $s = u_i$

p. 184, lfb 13

**Error:** *having  $P$*

**Correction:** *having  $P(x)$*

p. 197, lfb 12

**Error:** Some Immediate Action Enabled

**Correction:** Some Immediate Transition Enabled